

# Third Grade Standards

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These are the standards for what is taught throughout the year in Third Grade. It is the expectation that these skills will be reinforced after they have been taught.

Mathematical Practice Standards Taught Throughout the Year		
1. Make sense of problems and persevere in solving them	2. Reason abstractly and quantitatively	3. Construct viable arguments and critique the reasoning of others
<p>In Grade 3, mathematically proficient students know that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Students may use concrete objects, pictures, or drawings to help them conceptualize and solve problems, such as “Jim purchased 5 packages of muffins. Each package contained 3 muffins. How many muffins did Jim purchase?” or “Describe another situation where there would be 5 groups of 3 or <math>5 \times 3</math>.” Students may check their thinking by asking themselves, “Does this make sense?” Students listen to other students’ strategies and are able to make connections between various methods for a given problem.</p>	<p>Third graders should recognize that a number represents a specific quantity. They connect the quantity to written symbols and create a logical representation of the problem at hand, considering both the appropriate units involved and the meaning of quantities. For example: students apply their understanding of the meaning of the equal sign as “the same as” to interpret an equation with an unknown. When given <math>4 \times \square = 40</math>, they might think:</p> <ul style="list-style-type: none"> <li>• 4 groups of some number is the same as 40</li> <li>• 4 times some number is the same as 40</li> <li>• I know that 4 groups of 10 is 40 so the unknown number is 10</li> <li>• The missing factor is 10 because 4 times 10 equals 40.</li> </ul> <p>Teachers might ask, “How do you know” or “What is the relationship between the quantities?” to reinforce students’ reasoning and understanding.</p>	<p>Students may construct arguments using concrete referents, such as objects, pictures, and drawings. They refine their mathematical communication skills as they participate in mathematical discussions that the teacher facilitates by asking questions such as “How did you get that?” and “Why is that true?” Students explain their thinking to others and respond to others’ thinking. For example, after investigating patterns on the 100s chart, students might explain why the pattern makes sense.</p>



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Mathematical Practice Standards Taught Throughout the Year		
4. Model with mathematics	5. Use appropriate tools strategically	6. Attend to precision
<p>Students experiment with representing problem situations in multiple ways including numbers, words (mathematical language), drawing pictures, using objects, acting out, making a chart, list, or graph, creating equations, etc. Students need opportunities to connect the different representations and explain the connections. They should be able to use all of these representations as needed. Third graders should evaluate their results in the context of the situation and reflect on whether the results make sense. For example, students use various contexts and a variety of models (e.g., circles, squares, rectangles, fraction bars, and number lines) to represent and develop understanding of fractions. Students use models to represent both equations and story problems and can explain their thinking. They evaluate their results in the context of the situation and reflect on whether the results make sense. Students</p>	<p>Third graders consider the available tools (including drawings and estimation) when solving a mathematical problem and decide when certain tools might be helpful. For instance, they may use graph paper to find all the possible rectangles that have a given perimeter. They compile the possibilities into an organized list or a table, and determine whether they have all the possible rectangles. Students should be encouraged to answer questions such as, “Why was it helpful to use ___?”</p>	<p>As third graders develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and in their own reasoning. They are careful about specifying units of measure and state the meaning of the symbols they choose. For instance, when figuring out the area of a rectangle they record their answers in square units.</p>



<p>should be encouraged to answer questions, such as “What math drawing or diagram could you make and label to represent the problem?” or “What are some ways to represent the quantities?”</p>		
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<p align="center"><b>Mathematical Practice Standards Taught Throughout the Year</b></p>	
<p align="center"><b>7. Look for and make use of structure</b></p>	<p align="center"><b>8. Look for and express regularity in repeated reasoning</b></p>
<p>Students look closely to discover a pattern or structure. For instance, students use properties of operations (e.g., commutative and distributive properties) as strategies to multiply and divide. Teachers might ask, “What do you notice when ___?” or “How do you know if something is a pattern?”</p>	<p>Students in third grade should notice repetitive actions in computation and look for more shortcut methods. For example, students may use the distributive property as a strategy for using products they know to solve products that they don’t know. For example, if students are asked to find the product of <math>7 \times 8</math>, they might decompose 7 into 5 and 2 and then multiply <math>5 \times 8</math> and <math>2 \times 8</math> to arrive at <math>40 + 16</math> or 56. In addition, third graders continually evaluate their work by asking themselves, “Does this make sense? Students should be encouraged to answer questions, such as, “What is happening in this situation?” or “What predictions or generalizations can this pattern support?”</p>

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Standards taught during 1st Quarter		
<p><b>Operations and Algebraic Thinking</b> Represent and solve problems involving multiplication and division. Understand properties of multiplication and the relationship between multiplication and division. Multiply and divide within 100. Solve problems involving the four operations, and identify and explain patterns in arithmetic.</p>	<p><b>Number and Operations in Base Ten</b> Use place value understanding and properties of operations to perform multi-digit arithmetic. A range of strategies and algorithms may be used.</p>	<p><b>Measurement and Data</b> Geometric measurement: understand concepts of area and relate area to multiplication and addition.</p>
<p><b>3.OA.1</b> Interpret products of whole numbers, e.g., interpret <math>5 \times 7</math> as the total number of objects in 5 groups of 7 objects each. (Note: These standards are written with the convention that <math>a \times b</math> means <math>a</math> groups of <math>b</math> objects each; however, because of the commutative property, students may also interpret <math>5 \times 7</math> as the total number of objects in 7 groups of 5 objects each).</p> <p><b>3.OA.2</b> Interpret whole-number quotients of whole numbers, e.g., interpret <math>56 \div 8</math> as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. <i>For example, describe a context in which a number of shares or a number of</i></p>	<p><b>3.NBT.2</b> Fluently add and subtract within 1,000 using strategies and algorithms <sup>G</sup> based on place value, properties of operations, and/or the relationship between addition and subtraction.</p> <p><b>3.NBT.3</b> Multiply one-digit whole numbers by multiples of 10 in the range 10–90, e.g., <math>9 \times 80</math>, <math>5 \times 60</math> using strategies based on place value and properties of operations.</p>	<p><b>3.MD.7</b> Relate area to the operations of multiplication and addition.</p> <ol style="list-style-type: none"> <li>Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.</li> <li>Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real-world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.</li> <li>Use tiling to show in a concrete case that the area of a rectangle</li> </ol>



groups can be expressed as  $56 \div 8$ .

**3.OA.3** Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem. See Table 2, page 96. Drawings need not show details, but should show the mathematics in the problem. (This applies wherever drawings are mentioned in the Standards.)

**3.OA.4** Determine the unknown whole number in a multiplication or division equation relating three whole numbers. *For example, determine the unknown number that makes the equation true in each of the equations  $8 \times \square = 48$ ,  $5 = \square \div 3$ ,  $6 \times 6 = \square$ .*

**3.OA.5** Apply properties of operations as strategies to multiply and divide. *For example, if  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known (Commutative Property of Multiplication);  $3 \times 5 \times 2$  can be found by  $3 \times 5 = 15$ , then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 = 30$  (Associative Property of Multiplication); knowing that  $8 \times 5 = 40$  and  $8 \times 2 = 16$ , one can find  $8 \times 7$  as  $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$*

with whole number side lengths  $a$  and  $b + c$  is the sum of  $a \times b$  and  $a \times c$  (represent the distributive property with visual models including an area model).

d. Recognize area as additive. Find the area of figures composed of rectangles by decomposing into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real-world problems.

*(Distributive Property)*. Students need not use formal terms for these properties.

**3.OA.6** Understand division as an unknown-factor problem. *For example, find  $32 \div 8$  by finding the number that makes 32 when multiplied by 8.*

**3.OA.7** Fluently <sup>G</sup> multiply and divide within 100, using strategies such as the relationship between multiplication and division, e.g., knowing that  $8 \times 5 = 40$ , one knows  $40 \div 5 = 8$ , or properties of operations. Limit to division without remainders. By the end of Grade 3, know from memory all products of two one-digit numbers.

**3.OA.8** Solve two-step word problems using the four operations. Represent these problems using equations with a letter or a symbol, which stands for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. This standard is limited to problems posed with whole numbers and having whole-number answers. Students may use parentheses for clarification since algebraic order of operations is not expected.

**3.OA.9** Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using

<p>properties of operations. <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i></p>		
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Standards taught during 2 <sup>nd</sup> Quarter			
Operations and Algebraic Thinking Multiply and divide within 100.	Number and Operations in Base Ten Use place value understanding and properties of operations to perform multi-digit arithmetic. A range of strategies and algorithms may be used.	Number and Operations- Fractions Develop understanding of fractions as numbers. Grade 3 expectations in this domain are limited to fractions with denominators 2, 3, 4, 6, and 8.	Measurement and Data Represent and interpret data.
<p><b>3.OA.7</b> Fluently <sup>G</sup> multiply and divide within 100, using strategies such as the relationship between multiplication and division, e.g., knowing that <math>8 \times 5 = 40</math>, one knows <math>40 \div 5 = 8</math>, or properties of operations. Limit to division without remainders. By the end of Grade 3, know from memory all products of two one-digit numbers.</p>	<p><b>3.NBT.2</b> Fluently add and subtract within 1,000 using strategies and algorithms <sup>G</sup> based on place value, properties of operations, and/or the relationship between addition and subtraction.</p>	<p><b>3.NF.1</b> Understand a fraction <math>\frac{1}{b}</math> as the quantity formed by 1 part when a whole is partitioned into <math>b</math> equal parts; understand a fraction <math>\frac{a}{b}</math> as the quantity formed by <math>a</math> parts of size <math>\frac{1}{b}</math>.</p> <p><b>3.NF.2</b> Understand a fraction as a number on the number line; represent fractions on a number line diagram <sup>G</sup>.</p> <p>a. Represent a fraction <math>\frac{1}{b}</math> on a number line diagram defining the interval from 0 to 1 as the whole and partitioning it into <math>b</math> equal parts. Recognize that each part has size <math>\frac{1}{b}</math> and that the endpoint of the part based at 0 locates the number <math>\frac{1}{b}</math>.</p>	<p><b>3.MD.4</b> Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by creating a line plot <sup>G</sup>, where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.</p>





		<p>on the number line.</p> <p>b. Represent a fraction <math>\frac{a}{b}</math> (which may be greater than 1) on a number line diagram by marking off <math>a</math> lengths <math>\frac{1}{b}</math> from 0. Recognize that the resulting interval has size <math>\frac{a}{b}</math> and that its endpoint locates the number <math>\frac{a}{b}</math> on the number line.</p> <p><b>3.NF.3</b> Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.</p> <p>a. Understand two fractions as equivalent (equal) if they are the same size or the same point on a number line.</p> <p>b. Recognize and generate simple equivalent fractions, e.g., <math>\frac{1}{2} = \frac{2}{4}</math>, <math>\frac{4}{6} = \frac{2}{3}</math>. Explain why the fractions are equivalent, e.g., by using a visual fraction model<sup>G</sup>.</p> <p>c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. <i>Examples: Express 3 in the form <math>3 = \frac{3}{1}</math>; recognize that <math>\frac{6}{1} = 6</math>; locate <math>\frac{4}{4}</math> and 1 at the same point of a number line</i></p>	
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		<p><i>diagram.</i></p> <p>d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols <math>&gt;</math>, <math>=</math>, or <math>&lt;</math>, and justify the conclusions e.g., by using a visual fraction model.</p>	
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Standards taught during 3rd Quarter				
Operations and Algebraic Thinking Multiply and divide within 100. Solve problems involving the four operations, and identify and explain patterns in arithmetic.	Number and Operations in Base Ten Use place value understanding and properties of operations to perform multi-digit arithmetic. A range of strategies and algorithms may be used.	Number and Operations- Fractions Develop understanding of fractions as numbers. Grade 3 expectations in this domain are limited to fractions with denominators 2, 3, 4, 6, and 8.	Measurement and Data Geometric measurement: understand concepts of area and relate area to multiplication and addition. Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.	Geometry Reason with shapes and their attributes.
<p><b>3.OA.7</b> Fluently<sup>G</sup> multiply and divide within 100, using strategies such as the relationship between multiplication and division, e.g., knowing that <math>8 \times 5 = 40</math>, one knows <math>40 \div 5 = 8</math>, or properties of operations. Limit to division without remainders. By the end of Grade 3, know from memory all products of</p>	<p><b>3.NBT.2</b> Fluently add and subtract within 1,000 using strategies and algorithms<sup>G</sup> based on place value, properties of operations, and/or the relationship between addition and subtraction.</p>	<p><b>3.NF.1</b> Understand a fraction <math>\frac{1}{b}</math> as the quantity formed by 1 part when a whole is partitioned into <math>b</math> equal parts; understand a fraction <math>\frac{a}{b}</math> as the quantity formed by <math>a</math> parts of size <math>\frac{1}{b}</math>.</p> <p><b>3.NF.2</b> Understand a fraction as a number on the number line; represent fractions on a number line diagram<sup>G</sup>.</p> <p>a. Represent a fraction <math>\frac{1}{b}</math></p>	<p><b>3.MD.5</b> Recognize area as an attribute of plane figures and understand concepts of area measurement.</p> <p>a. A square with side length 1 unit, called “a unit square”, is said to have “one square unit” of area, and can be used to measure area.</p> <p>b. A plane figure which can be covered without gaps or overlaps by <math>n</math> unit squares is said to have an area of <math>n</math> square</p>	<p><b>3.G.1</b> Draw and describe triangles, quadrilaterals (rhombuses, rectangles, and squares), and polygons (up to 8 sides) based on the number of sides and the presence or absence of square corners (right angles).</p> <p><b>3.G.2</b> Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. <i>For</i></p>



<p>two one-digit numbers.</p> <p><b>3.OA.8</b> Solve two-step word problems using the four operations. Represent these problems using equations with a letter or a symbol, which stands for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. This standard is limited to problems posed with whole numbers and having whole-number answers. Students may use parentheses for clarification since algebraic order of operations is not expected.</p>		<p>on a number line diagram defining the interval from 0 to 1 as the whole and partitioning it into <math>b</math> equal parts. Recognize that each part has size <math>\frac{1}{b}</math> and that the endpoint of the part based at 0 locates the number <math>\frac{1}{b}</math> on the number line.</p> <p>b. Represent a fraction <math>\frac{a}{b}</math> (which may be greater than 1) on a number line diagram by marking off <math>a</math> lengths <math>\frac{1}{b}</math> from 0. Recognize that the resulting interval has size <math>\frac{a}{b}</math> and that its endpoint locates the number <math>\frac{a}{b}</math> on the number line.</p> <p><b>3.NF.3</b> Explain equivalence of fractions in special cases, and compare fractions by reasoning</p>	<p>units.</p> <p><b>3.MD.6</b> Measure areas by counting unit squares (square cm, square m, square in, square ft., and improvised units).</p> <p><b>3.MD.7</b> Relate area to the operations of multiplication and addition.</p> <p>a. Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.</p> <p>b. Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real-world and mathematical problems, and represent whole-number products as rectangular areas in mathematical</p>	<p><i>example, partition a shape into 4 parts with equal area, and describe the area of each part as <math>\frac{1}{4}</math> of the area of the shape.</i></p>
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		<p>about their size.</p> <p>a. Understand two fractions as equivalent (equal) if they are the same size or the same point on a number line.</p> <p>b. Recognize and generate simple equivalent fractions, e.g., <math>\frac{1}{2} = \frac{2}{4}</math>, <math>\frac{4}{6} = \frac{2}{3}</math>. Explain why the fractions are equivalent, e.g., by using a visual fraction model <sup>G</sup>.</p> <p>c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. <i>Examples: Express 3 in the form <math>3 = \frac{3}{1}</math>; recognize that <math>\frac{6}{1} = 6</math>; locate <math>\frac{4}{4}</math> and 1 at the same point of a number line diagram.</i></p> <p>d. Compare two fractions with the same numerator or</p>	<p>reasoning.</p> <p>c. Use tiling to show in a concrete case that the area of a rectangle with whole number side lengths <math>a</math> and <math>b + c</math> is the sum of <math>a \times b</math> and <math>a \times c</math> (represent the distributive property with visual models including an area model).</p> <p>d. Recognize area as additive. Find the area of figures composed of rectangles by decomposing into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real-world problems.</p> <p><b>3.MD.8</b> Solve real-world and mathematical problems involving perimeters of polygons, including finding</p>	
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		<p>the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols <math>&gt;</math>, <math>=</math>, or <math>&lt;</math>, and justify the conclusions e.g., by using a visual fraction model.</p>	<p>the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.</p>	
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Standards taught during 4 <sup>th</sup> Quarter		
Operations and Algebraic Thinking Multiply and divide within 100. Solve problems involving the four operations, and identify and explain patterns in arithmetic.	Numbers and Operations in Base Ten Use place value understanding and properties of operations to perform multi-digit arithmetic. A range of strategies and algorithms may be used.	Measurement and Data Solve problems involving money, measurement, and estimation of intervals of time, liquid volumes, and masses of objects. Represent and interpret data.
<p><b>3.OA.7</b> Fluently <sup>G</sup> multiply and divide within 100, using strategies such as the relationship between multiplication and division, e.g., knowing that <math>8 \times 5 = 40</math>, one knows <math>40 \div 5 = 8</math>, or properties of operations. Limit to division without remainders. By the end of Grade 3, know from memory all products of two one-digit numbers.</p> <p><b>3.OA.8</b> Solve two-step word problems using the four operations. Represent these problems using equations with a letter or a symbol, which stands for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. This standard is limited to problems posed with whole numbers and having whole-number answers. Students may use parentheses for clarification since algebraic</p>	<p><b>3.NBT.1</b> Use place value understanding to round whole numbers to the nearest 10 or 100.</p> <p><b>3.NBT.2</b> Fluently add and subtract within 1,000 using strategies and algorithms <sup>G</sup> based on place value, properties of operations, and/or the relationship between addition and subtraction.</p>	<p><b>3.MD.1</b> Work with time and money.</p> <p>a. Tell and write time to the nearest minute. Measure time intervals in minutes (within 90 minutes). Solve real-world problems involving addition and subtraction of time intervals (elapsed time) in minutes, e.g., by representing the problem on a number line diagram or clock.</p> <p>b. Solve word problems by adding and subtracting within 1,000, dollars with dollars and cents with cents (not using dollars and cents simultaneously) using the \$ and ¢ symbol appropriately (not including decimal notation).</p> <p><b>3.MD.2</b> Measure and estimate liquid volumes and masses of objects using standard units of grams, kilograms, and</p>

<p>order of operations is not expected.</p>		<p>liters. Add, subtract, multiply, or divide whole numbers to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem. Excludes multiplicative comparison problems involving notions of "times as much"; see Table 2, page 96.</p> <p><b>3.MD.3</b> Create scaled picture graphs to represent a data set with several categories. Create scaled bar graphs to represent a data set with several categories. Solve two-step "how many more" and "how many less" problems using information presented in the scaled graphs. <i>For example, create a bar graph in which each square in the bar graph might represent 5 pets, then determine how many more/less in two given categories.</i></p>
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